

## PROBLEM SHEET 3

## Alternating current

1. A wire frame of area  $S = 0.1 \text{ m}^2$  is rotated with frequency  $f = 100 \text{ Hz}$  in magnetic field of induction  $B = 2 \text{ T}$ . For the induced alternating EMF, determine:
  - a) Angular frequency  $\omega$ ;
  - b) Period  $T$ ;
  - c) Amplitude  $\mathcal{E}_m$ ;
  - d) Peak-to-peak amplitude  $\mathcal{E}_{pp}$ ;
  - e) R.m.s. amplitude  $\mathcal{E}$ .
2. A  $100 \Omega$  resistor is connected to a power source of  $100 \text{ V}$  a.c. Determine:
  - a) Effective current;
  - b) Amplitudes of current and voltage;
  - c) Peak-to-peak amplitudes of current and voltage.
3. For a power source of  $100 \text{ V}$  at  $50 \text{ Hz}$ , the instantaneous value of voltage at the initial moment of time  $t = 0$  is zero. Determine the instantaneous values of voltage and phase after:
  - a)  $1/12$  of a cycle; b)  $1/8$  of a cycle; c)  $1/6$  of a cycle; d)  $1/4$  of a cycle;
  - e)  $1/3$  of a cycle; f)  $3/8$  of a cycle; g)  $5/12$  of a cycle; h)  $1/2$  of a cycle.

Express the phase both in radians and in degrees.
4. A  $75 \Omega$  resistor is connected to a power source of  $150 \text{ V}$  at  $50 \text{ Hz}$ . At the initial moment of time  $t = 0$ , the instantaneous value of the voltage was zero, and that of the current was  $2 \text{ A}$ . Determine:
  - a) Phase shift  $\varphi$  between voltage and current;
  - b) Time interval  $\Delta t$  which corresponds to this phase shift;
  - c) Power factor;
  - d) Apparent power;
  - e) Active power consumed in the resistor.
5. **ASSIGNMENT.** A  $100 \Omega$  resistor is connected to a power source of  $100 \text{ V}$  at  $50 \text{ Hz}$ . At the initial moment of time  $t = 0$ , the instantaneous value of the voltage was zero, and that of the current was  $0.7 \text{ A}$ . Determine:
  - a) Phase shift  $\varphi$  between voltage and current;
  - b) Time interval  $\Delta t$  which corresponds to this phase shift;
  - c) Power factor;
  - d) Apparent power;
  - e) Active power consumed in the resistor.
6. (\*) For a power source of  $100 \text{ V}$  a.c., determine the average value of voltage over one half-cycle. For this, you will need to take integral of voltage over a half-cycle. See more details in the textbook.